



# Predicting Human Mobility via Graph Convolutional Dual-attentive Networks

Weizhen Dang  
Tsinghua University  
Beijing, China  
dangweizhen@126.com

Haibo Wang\*  
Tsinghua University  
Beijing, China  
hbwang1994@gmail.com

Shirui Pan  
Monash University  
Australia  
shirui.pan@monash.edu

Pei Zhang  
Beijing University of Posts and  
Telecommunications  
Beijing, China  
zhangpei@bupt.edu.cn

Chuan Zhou  
Chinese Academy of Sciences  
Beijing, China  
zhouchuan@amss.ac.cn

Xin Chen  
Tsinghua University  
Beijing, China  
chenxinsteven@outlook.com

Jilong Wang  
Tsinghua University  
Beijing, China  
wjl@cernet.edu.cn

WSDM 2022

Code: <https://github.com/GCDAN/GCDAN>

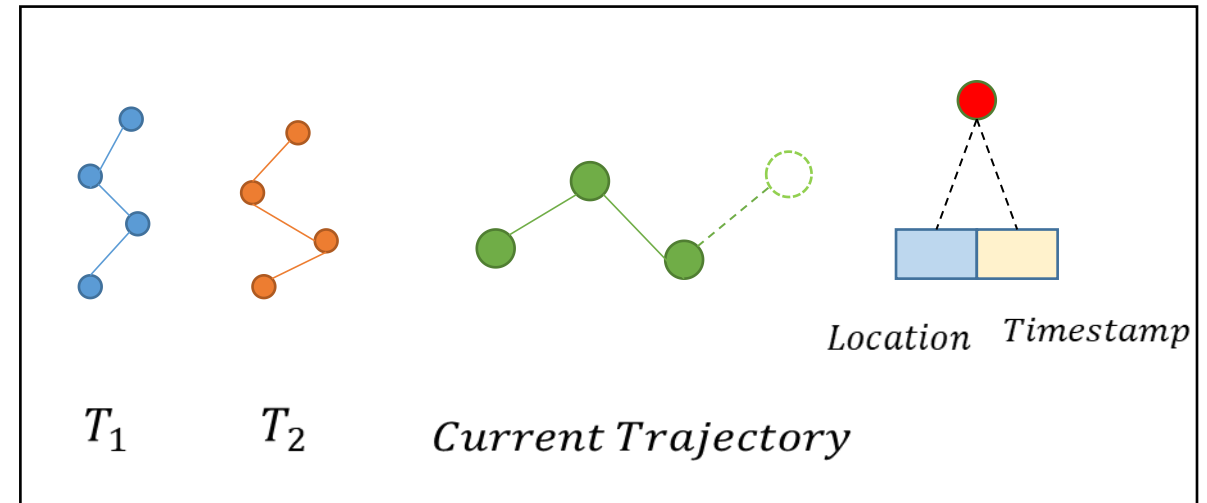


**Reported by Nengqiang Xiang**

# Introduction

Methods that already exist do not well cope with the **sparsity** and **inaccuracy** of trajectory data and the complicated **high-order nature** of the sequential dependency.

To solve the problems, this paper proposes a novel framework named Graph Convolutional Dual-attentive Networks (GCDAN).



An example for Human Mobility Predicting

# Method

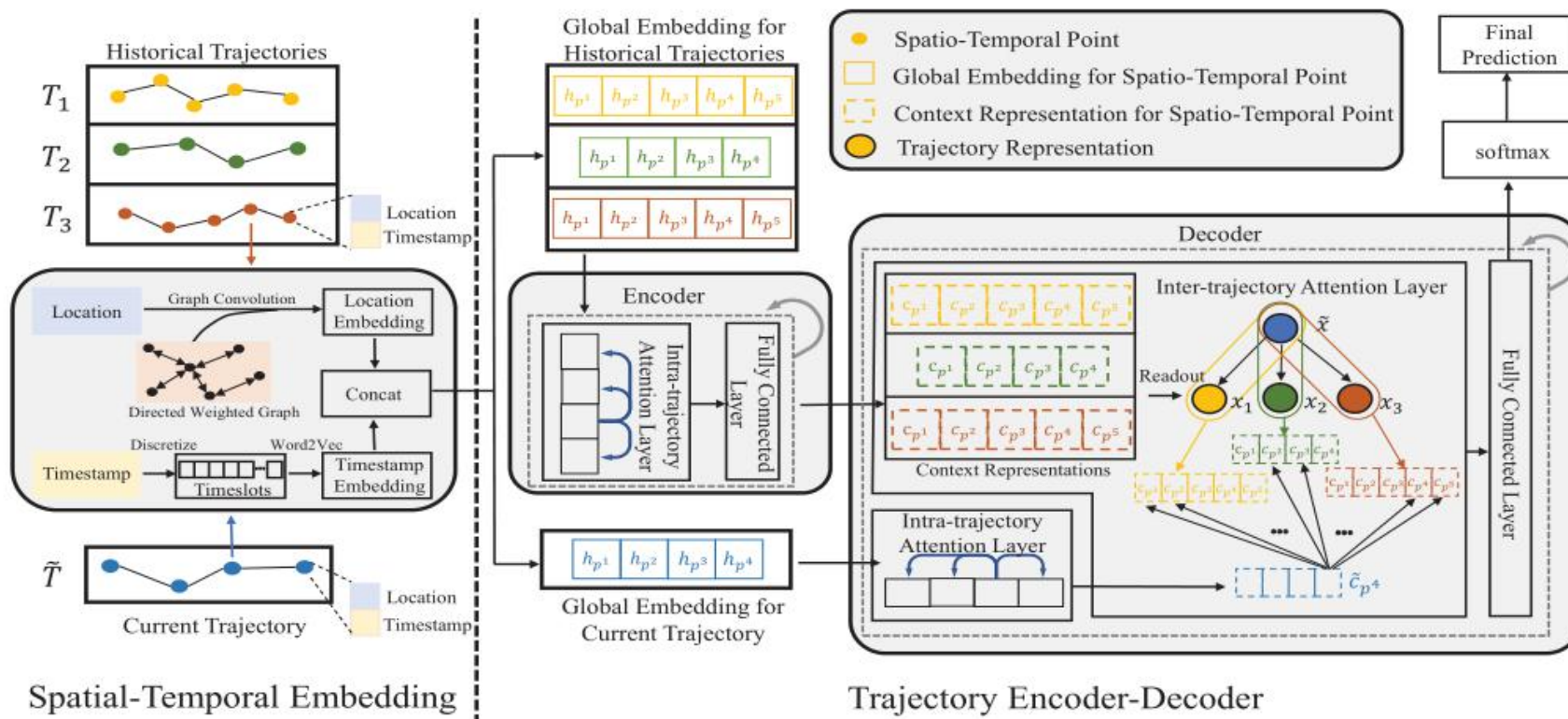


Figure 1: The overview of GCDAN. The spatial-temporal embedding module introduces the graph convolution and sparse embedding to learn representations of spatial-temporal points. The trajectory encoder-decoder module employs a dual-attentive mechanism. The intra-trajectory attention layer models the sequential dependence within a trajectory and generates the context representation for each spatial-temporal point. The inter-trajectory attention layer models the correlation between the historical trajectories and current trajectory and generates the final prediction.

## Method

### Problem Formulation

location identifiers:  $L = \{l_1, l_2, \dots, l_{|L|}\}$

spatio-temporal point:  $p = (l, t)$

user:  $U = \{u_1, u_2, \dots, u_{|U|}\}$

trajectory:  $T_u = p_u^1 p_u^2 \dots p_u^m$

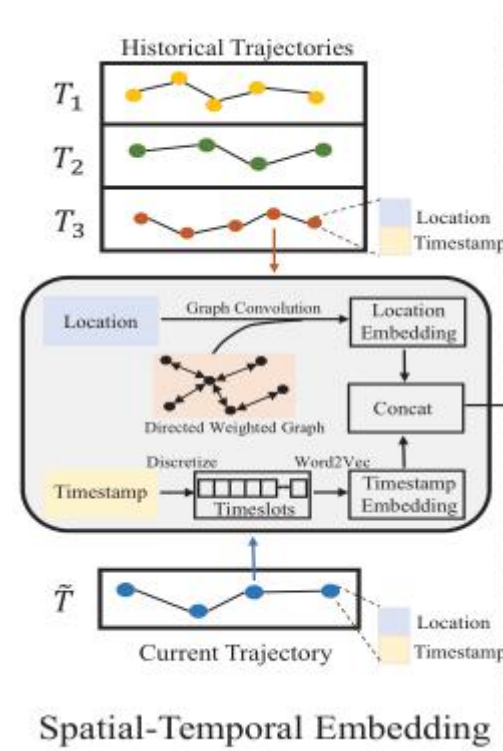
historical trajectories:  $S_u = \{T_u^1, T_u^2, \dots, T_u^{|S_u|}\}$

current trajectory:  $\tilde{T}_u = p_u^1 p_u^2 \dots p_u^n$

### Spatio-temporal Embedding Module

Timestamp Embedding:

$$\mathbf{h}_t = \Theta_T \mathbf{v}_t$$



## Method

### Location Embedding:

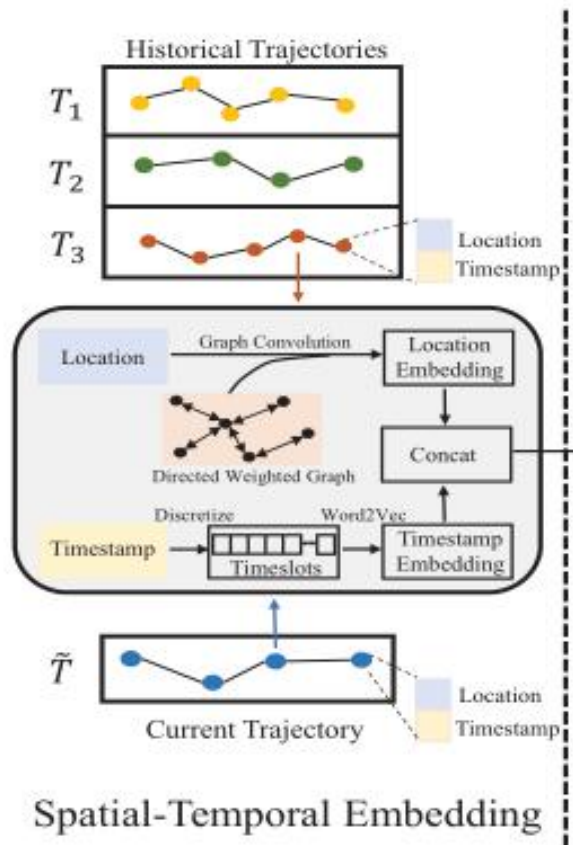
$$\begin{cases} w_{ij} = \frac{c_{ij}}{\sum_{l_r \in L} c_{ir}} & \frac{c_{ij}}{\sum_{l_r \in L} c_{ir}} > \frac{1}{|L|}, \\ w_{ij} = 0 & \text{otherwise,} \end{cases} \quad c_{ij} = (l_i, l_j) \quad (1)$$

$$H_L = \sum_{k=0}^{K-1} \sigma \left( (D_O^{-1} W)^k V_L \Theta_k^0 + (D_I^{-1} W^T)^k V_L \Theta_k^1 \right), \quad (2)$$

$$D_O = \text{diag}(W\mathbf{1}) \text{ and } D_I = \text{diag}(W^T\mathbf{1})$$

$$H_L = (h_{l_1}, \dots, h_{l_{|L|}})^T \quad H_L \in \mathbb{R}^{|L| \times d_2}$$

$$\Theta_k^0 \in \mathbb{R}^{|L| \times d_2} \text{ and } \Theta_k^1 \in \mathbb{R}^{|L| \times d_2}$$



## Method

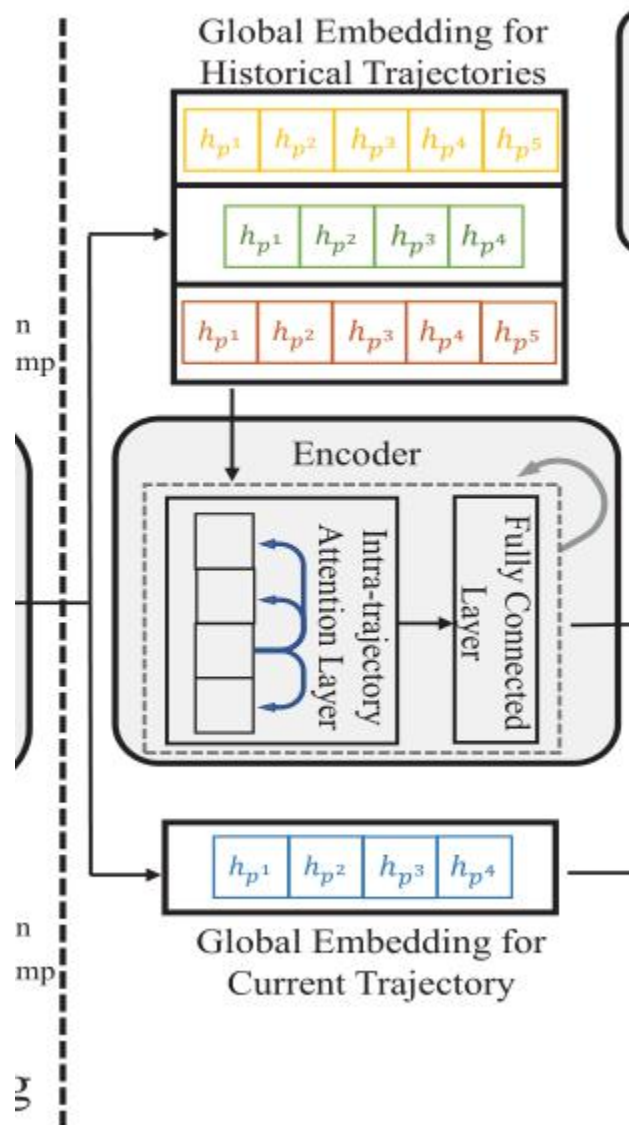
Global Embedding:

$$\mathbf{h}_p = \mathbf{h}_t \parallel \mathbf{h}_l \quad \mathbf{h}_p \in \mathbb{R}^{d_1+d_2}$$

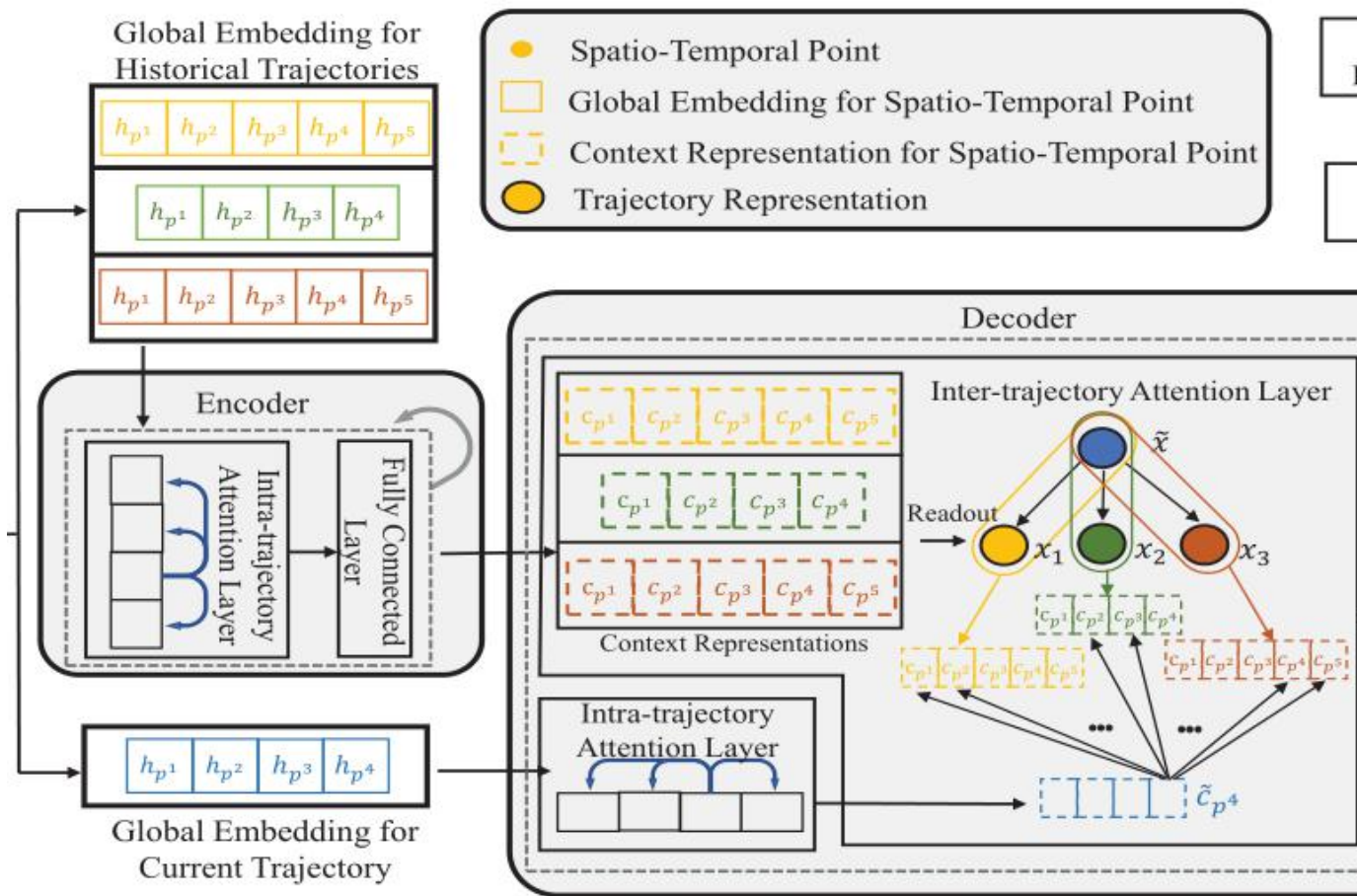
Trajectory Position Coding:

$$\text{pos}_i(j) = \cos \left( \frac{i}{C \frac{j-(j\%2)}{d_1+d_2}} - \frac{(j\%2)\pi}{2} \right); \quad (3)$$

$$\mathbf{h}_{p^i} = \mathbf{h}_{p^i} + \text{pos}_i$$



# Method



Trajectory Encoder-Decoder

## Trajectory Encoder-decoder Module

Encoder:

$$sim_p(\mathbf{h}_{p^i}, \mathbf{h}_{p^j}) = \frac{\exp(f(\mathbf{h}_{p^i}, \mathbf{h}_{p^j}))}{\sum_{r=1}^m \exp(f(\mathbf{h}_{p^i}, \mathbf{h}_{p^r}))}, \quad (4)$$

$$\mathbf{c}_{p^i} = \sum_{j=1}^m sim_p(\mathbf{h}_{p^i}, \mathbf{h}_{p^j}) \mathbf{h}_{p^j}, \quad (5)$$

Decoder:

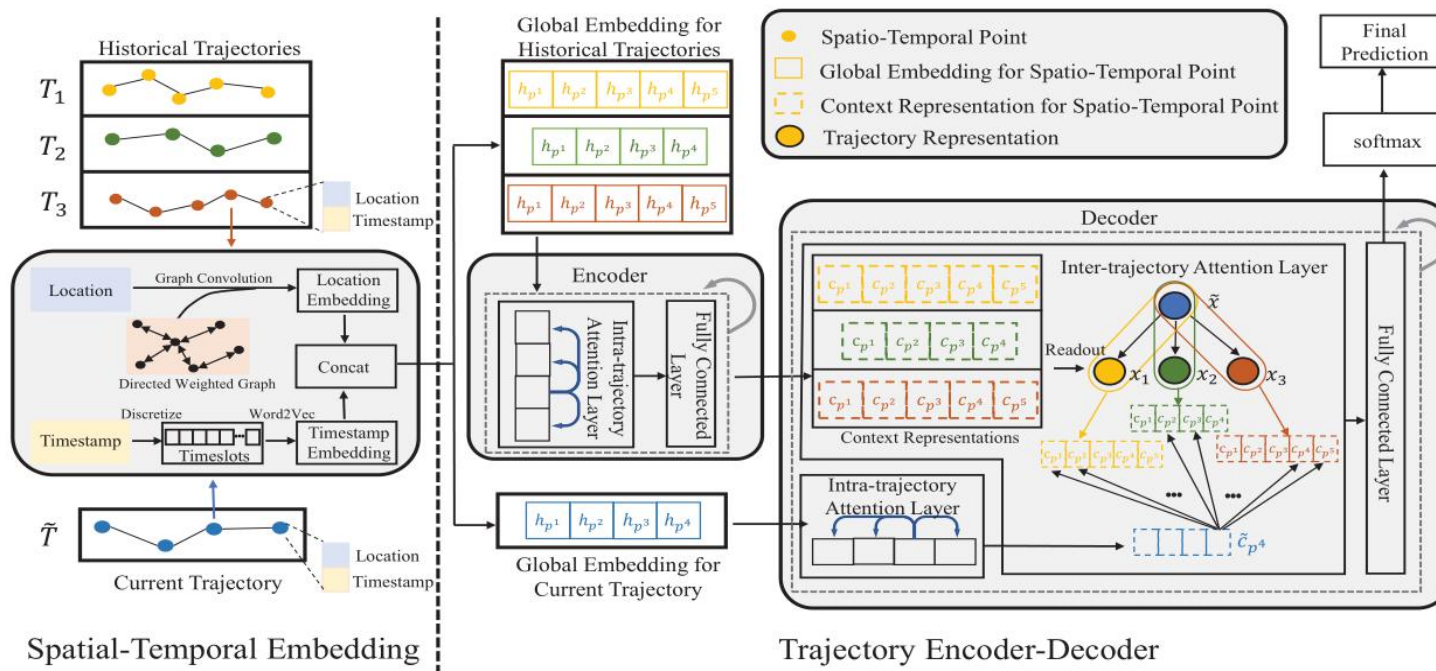
$$\mathbf{x} = \frac{1}{m} \sum_{j=1}^m \mathbf{c}_{p^j}, \quad (6)$$

$$sim_t(\tilde{\mathbf{x}}, \mathbf{x}_i) = \frac{\exp(f(\tilde{\mathbf{x}}, \mathbf{x}_i))}{\sum_{r=1}^{|S|} \exp(f(\tilde{\mathbf{x}}, \mathbf{x}_r))}, \quad (7)$$

$$\mathbf{v}_{p^n} = \sum_{i=1}^{|S|} sim_t(\tilde{\mathbf{x}}, \mathbf{x}_i) \sum_{j=1}^m sim_p(\tilde{\mathbf{c}}_{p^n}, \mathbf{c}_{p^j}) \mathbf{c}_{p^j}, \quad (8)$$

# Method

## Objective Function



$$\hat{y} = \text{softmax}(\hat{\Theta}v_{p^n}), \quad (9)$$

$$\mathcal{L}_c = - \sum_{u \in U} \sum_{i=1}^{|L|} y_u^i \log \hat{y}_u^i, \quad (10)$$

$$\mathcal{L} = \mathcal{L}_c + \alpha \mathcal{L}_{reg}, \quad (11)$$

Figure 1: The overview of GCDAN. The spatial-temporal embedding module introduces the graph convolution and sparse embedding to learn representations of spatial-temporal points. The trajectory encoder-decoder module employs a dual-attentive mechanism. The intra-trajectory attention layer models the sequential dependence within a trajectory and generates the context representation for each spatial-temporal point. The inter-trajectory attention layer models the correlation between the historical trajectories and current trajectory and generates the final prediction.



# Experiments

**Table 1: Dataset statistics.**

Dataset	Gowalla	Foursquare	WiFi-Trace
Time duration	1 year	1 year	2 week
Users	857	886	3642
#(Record)	129679	82575	1011049
#(Trajectory)	8568	7974	41937
#(Location)	20006	10497	251

for each dataset. In our experiments, we select the first 75% of trajectories for each user as the training data and the rest 25% as the testing data. In addition, 10% of the training data is used as the validation data.

# Experiments

**Table 2: Gowalla**

Metrics	MC	FPMC	LSTM	ST-RNN	DeepMove	GCDAN
Acc@1	0.1188	0.1204	0.1252	0.1279	0.1338	<b>0.1377</b>
Acc@5	0.2056	0.2066	0.2453	0.2568	0.2731	<b>0.3086</b>
Acc@10	0.2306	0.2307	0.2907	0.3112	0.3299	<b>0.3780</b>

**Table 3: Foursquare**

Metrics	MC	FPMC	LSTM	ST-RNN	DeepMove	GCDAN
Acc@1	0.0818	0.0835	0.0912	0.1057	0.1245	<b>0.1613</b>
Acc@5	0.1753	0.1762	0.1824	0.2368	0.2790	<b>0.3417</b>
Acc@10	0.2252	0.2257	0.2120	0.2787	0.3360	<b>0.4093</b>

**Table 4: WiFi-Trace**

Metrics	MC	FPMC	LSTM	ST-RNN	DeepMove	GCDAN
Acc@1	0.1612	0.3231	0.5685	0.5702	0.5729	<b>0.5912</b>
Acc@5	0.3173	0.5169	0.7821	0.7918	0.8030	<b>0.8064</b>
Acc@10	0.3882	0.6843	0.8473	0.8523	0.8707	<b>0.8726</b>

# Experiments

**Table 5: Ablation Study.**

	Gowalla	Foursquare	WiFi-Trace
GCDAN-base	0.1311	0.1580	0.5768
GCDAN-tc	0.1340	0.1607	0.5815
GCDAN-gc	0.1336	0.1597	0.5895
GCDAN-full	0.1377	0.1613	0.5912

The above experimental results demonstrate the effectiveness and superiority of GCDAN.

# Experiments

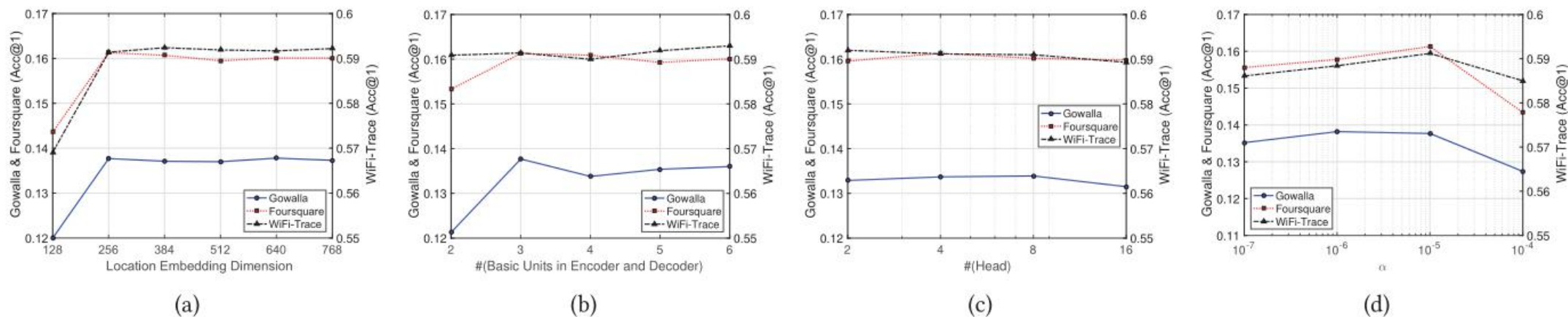


Figure 2: Results of parameter sensitivity *w.r.t.* (a) the location embedding dimension, (b) the number of basic units in encoder and decoder, (c) the number of heads of the multi-head attention mechanism and (d) the balance hyper-parameter  $\alpha$  in Eq. (11)



# Thanks